

**B.Sc. MATHEMATICS
FIRST SEMESTER
CALCULUS
BSM – 101 IDMi**

[USE OMR SHEET FOR OBJECTIVE PART]

Duration: 3 hrs.

Full Marks: 70

Time: 30 min.

Marks: 20

Choose the correct answer from the following:

$$1 \times 20 = 20$$

1. Given $S = (0,1)$ and $a = 2$. Which of the following option is correct?

 - S is a nbd of 2
 - S is not a nbd of 2
 - S may or may not be a nbd of 2
 - None of the above

2. Given $S = (0,1)$. Is 0 is a limit point of S ?

 - YES
 - NO
 - YES if $0 \in (1,0)$
 - No if $0 \notin (0,1)$

3. Domain of $f(x) = \frac{1}{x}$ is what?

 - $R - \{1\}$
 - $R - \{-1\}$
 - R
 - $R - \{0\}$

4. $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} = ?$

 - 4
 - 0
 - 4
 - 2

5. The C.F of the equation $\frac{d^2y}{dx^2} + 9y = \cos 4x$ is

 - $C_1 \cos 3x - C_2 \sin 3x$
 - $C_1 \cos 3x + C_2 \sin 3x$
 - $-C_1 \cos 3x + C_2 \sin 3x$
 - $C_1 \cos 9x + C_2 \sin 9x$

6. Stationary point of $2x^3 - 3x^2 - 12x + 6$ are

 - $x = -1, 2$
 - $x = 1, 2$
 - $x = -1, -2$
 - $x = 1, -2$

1. If $y = \log x$, which of the following is fifth derivative $y_5 = ?$
- a. $y_5 = \frac{(-1)^4 \cdot 4}{x^4}$
 - b. $y_5 = \frac{(-1)^4 \cdot 4}{x^5}$
 - c. $y_5 = \frac{24}{x^4}$
 - d. $y_5 = \frac{24}{x^5}$
2. If $f(x) = x + |x|$, $f(-3) = ?$
- a. -6
 - b. 6
 - c. 0
 - d. 3
3. Given $N = \{1, 2, 3, \dots\}$
- a. N is a closed set
 - b. N is an open set
 - c. N is not a closed set
 - d. N is not open set
4. Statement of Lagrange's mean value theorem is
- a. If a function f defined on $[a, b]$ is
 - (i) continuous on $[a, b]$
 - (ii) Derivable on (a, b) ,
 - (iii) $f(a) = f(b)$
 then there exist at least one real number c between a and b such that

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$
 - b. If a function f defined on $[a, b]$ is
 - (i) continuous on $[a, b]$
 - (ii) Derivable on (a, b) , then there exist at least one real number c between a and b such that $f'(c) = \frac{f(b) - f(a)}{b - a}$
 - c. If a function f defined on $[a, b]$ is
 - (i) continuous on $[a, b]$

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(ii) Derivable on $[a, b]$,

(iii) $f(a) = f(b)$

then there exist at least one real number c between a and b such that
 $f'(c) = 0$

d. If a function f defined on $[a, b]$ is

(i) continuous on $[a, b]$

(ii) Derivable on $[a, b]$, then there exist at least one real number c between a and b such that $f'(c) = 0$

11. $\int dx = ?$

a. dx

b. x

c. Both a and b

d. $x + c$, where c is arbitrary constant

12. Given $S = \{x : 0 \leq x \leq 1, x \in Q\}$, Then

a. S is a bounded above

b. S is not a bounded set

c. S is a bounded set

d. None of the above

13. Equation of tangent is

a. $y - y' = \frac{dy}{dx}(x - x')$

b. $y - y' = \frac{dx}{dy}(x - x')$

c. $x - x' = \frac{dy}{dx}(y - y')$

d. All of the above

14. Equation of normal is

a. $y - y' = \frac{dy}{dx}(x - x')$

b. $x - x' = \frac{dy}{dx}(y - y')$

c. $x - x' = \frac{dx}{dy}(y - y')$

d. None of the above

15. $\int \log x = ?$

- a. $\frac{1}{x}$
- b. x
- c. $x \log x + c$

d. None of the above

16. $\int \frac{\cos x - \sin x}{\sin x + \cos x} dx =$

- a. $\log(\sin x + \cos x)$
- b. $\log(\sin x - \cos x)$
- c. Both a and b

d. None of the above

17. A straight line that constantly approaches a given curve but does not meet at any infinite distance is called

- a. Tangent
- b. Normal
- c. Asymptote
- d. None of the above

18. Asymptotes may be

- a. Vertical
- b. Horizontal
- c. Oblique
- d. All of the above

19. How many tangents a parabola have

- a. One
- b. Two
- c. Four
- d. None of the above

20. $\int a^x dx =$

- a. $a^x \log_e a$
- b. $\log_e a$
- c. Both a and b
- d. None of the above

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(Descriptive)

Time : 2 hrs. 30 min.

Marks : 50

[Answer question no. 1 & any four (4) from the rest]

1. Define Asymptote. Also find all the asymptotes to the curve

10

$$f(x) = \frac{3x - 2}{x + 1}$$

2. Find the derivative of the following

5+5=10

a. $y = e^{2x} \sin x + x^3 \log x$

b. $y = \frac{1 - \cos x}{1 + \cos x}$

3. State and Prove Rolle's Theorem

2+8=10

4. Find the maximum or minimum value of $3x^4 + 8x^3 - 6x^2 + 24x + 1$

10

5. If $y = A \cos nx + B \sin nx$, show that $y_2 + n^2 y = 0$

10

6. a. Evaluate $\lim_{\substack{x \rightarrow 0 \\ y \rightarrow 0}} \frac{x^2 y}{x^4 + y^2}$

5+5=10

b. Discuss the continuity of

$$f(x, y) = \begin{cases} \frac{x}{\sqrt{x^2 + y^2}}, & x \neq 0, y \neq 0 \\ 2, & x = 0, y = 0 \end{cases} \text{ at the origin.}$$

7. a. Find the equation of tangent to the curve $xy^2 = 4(4 - x)$ at the point where it cuts the line $x = y$

10

8. Find the equation of normal to the curve $x = a(t - \sin t), y = a(1 - \cos t)$ at the point t

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